

JAYPEE UNIVERSITY OF INFORMATION TECHNOLOGY, WAKNAGHAT
 TEST -2 EXAMINATION- March-April 2017
 M.Tech IInd Semester

COURSE CODE: 10M11EC213

MAX. MARKS: 25

COURSE NAME: INFORMATION AND CODING THEORY

COURSE CREDITS: 03

MAX. TIME: 1.5 Hrs

Note: All questions are compulsory. Carrying of mobile phone during examinations will be treated as case of unfair means.

Q1

- (i) Consider the following binary sequence 11101001100010110100..... Use the Lempel-Ziv algorithm to encode this sequence. Assume that the binary symbols 0 and 1 are already in the codebook. **(3 Marks)**
- (ii) A voice-grade channel of the telephone network has a bandwidth of 3.4 kHz. Calculate
 - (a) The information capacity of the telephone channel for a SNR of 30 dB.
 - (b) The minimum SNR required to support information transmission through the telephone channel at the rate of 9600b/s. **(2 Marks)**

Q2

- (i) Prove that an (n,k) block code must have $d_{\min} \leq n-k+1$. Prove that if d_{\min} is odd, then all $(d_{\min}-1)/2$ error patterns can be corrected. **(3 Marks)**
- (ii) Define and explain a field. Highlight the properties of Galois Field. **(3 Marks)**

Q3

- (i) The parity check matrix for a particular (7,4) linear block code is given by **(5 Marks)**

$$H = \begin{bmatrix} 1 & 1 & 1 & 0 & 1 & 0 & 0 \\ 1 & 1 & 0 & 1 & 0 & 1 & 0 \\ 1 & 0 & 1 & 1 & 0 & 0 & 1 \end{bmatrix}$$

- (a) Find the generator matrix.
- (b) List out all the codewords.
- (c) What is the minimum distance between the code vectors?
- (d) How many errors can be detected and how many can be corrected?
- (ii) How are errors and erasures related in linear block codes? **(2 Marks)**

Q4

- (i) For the (5,1) repetition code $G = [1 \ 1 \ 1 \ 1 \ 1]$, evaluate the syndrome s for the following error patterns **(4 Marks)**
 - (a) All five possible single-error patterns
 - (b) All 10 possible double-error patterns.
- (ii) What are Cyclic Codes? Divide x^7+1 by x^3+x+1 over GF(2). **(3 Marks)**
