
Note: (a) All questions are compulsory.

(b) The candidate is allowed to make Suitable numeric assumptions wherever required for solving problems

Q.1 A solid circular shaft is subjected to a bending moment of 3kNm and a torque of 1kNm. The shaft is to be made in carbon steel for which (yield stress) $\sigma_y = 480\text{MPa}$ and (max shearing stress) $\tau_y = 265\text{MPa}$. If in the beginning plastic deformation is to be avoided, calculate the shaft diameter using: (a) Maximum Principal Stress Theory (b) Maximum Shearing Stress Theory (c) Distortion Energy Theory [6]

Q.2 The homogeneous three-dimensional state of stress for a metal part undergoing plastic deformation is defined as $\sigma_x = 10$, $\sigma_y = 20$, $\sigma_z = -10$. $\tau_{xy} = 5$, $\tau_{yz} = \tau_{zx} = 0$ (all in MPa). Using Von-Mises yield criterion find the value of estimated shear yield stress in MPa, also show Mohr Circle for the same. [7]

Q.3 A member made of isotropic bronze ($E = 82.6\text{ GPa}$ and $\nu = 0.35$) is subjected to a state of plane strain ($\epsilon_{zz} = \epsilon_{zx} = \epsilon_{zy} = 0$). Determine σ_{zz} , ϵ_{xx} , ϵ_{yy} , and $\gamma_{xy} = 2\epsilon_{xy}$, if $\sigma_{xx} = 90\text{ MPa}$, $\sigma_{yy} = -50\text{ MPa}$, and $\sigma_{xy} = -70\text{ MPa}$. [4]

Q.4 With help of neat diagram prove that cubical dilation $\Delta = \epsilon_{xx} + \epsilon_{yy} + \epsilon_{zz}$ [4]

Q.5 State the conditions under which the following is a possible system of strains: [4]

$$\begin{aligned}\epsilon_{xx} &= a + b(x^2 + y^2) + x^4 + y^4, & \gamma_{xy} &= 0 \\ \epsilon_{yy} &= \alpha + \beta(x^2 + y^2) + x^4 + y^4, & \gamma_{yz} &= 0 \\ \gamma_{xy} &= A + Bxy(x^2 + y^2 - c^2), & \epsilon_{zz} &= 0\end{aligned}$$