

Note: (a) All questions are compulsory.

(b) Marks are indicated against each question in square brackets.

(c) The candidate is allowed to make Suitable numeric assumptions wherever required for solving problems.

1. For the given Cobb-Douglas production function of a firm:

$$Q = f(L, K) = AL^\alpha K^\beta$$

Prove that:

(CO2) [2+3=5]

- (a) Elasticity of Factor Substitution (σ) is 1
(b) Marginal Product of Labour (MP_L) and Marginal Product of Capital (MP_K) are homogenous of degree 0, respectively.

2. Find the degree of homogeneity for the following production functions, and mention whether they exhibit increasing, decreasing or constant returns to scale: (CO3) [1X3=3]

- (a) $Q = f(L, K, T) = \frac{LK^2}{T} + 2LT$
(b) $Q = f(L, K) = 10L^{1/2} + 5K^{1/2}$
(c) $Q = f(L, K) = L^3 + 4L^2K + K^3$

3. The production function of a firm is given as $Q = 2L^{1/3}K^{2/3}$. The price of labour is Rs. 8 per unit and the price of capital is Rs. 2 per unit. Using the langrage method, find the cost-minimizing combination of labour and capital to produce 64 units of output? Also find, the total minimum cost for the firm. (CO3) [5]

4. Discuss the equilibrium of the industry in long run under perfect competition. (CO3) [4]

5. A monopolist sells his output in two different markets. His demand and cost functions are as follows: (CO4) [8]

Market I: $Q_1 = 21 - 0.1P_1$

Market II: $Q_2 = 50 - 0.4P_2$

$TC=C= 2000+10Q= 2000+10(Q_1 + Q_2)$

Find:

- What is the profit maximizing level of output (Q) produced by the monopolist (i) with discrimination, and (ii), without discrimination?
- What price (P) will the monopolist charge: (i) with discrimination, and (ii) without discrimination.
- Compare the profit differentials (II) between the discriminated market and non-discriminated market.
- Calculate the elasticity of demand (E_d) in discriminated markets.