

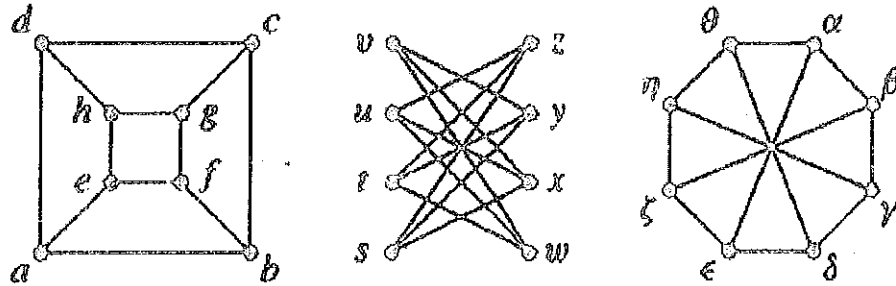
Note: All questions are compulsory. Marks are indicated against each question in square brackets.

1. [1.5 + 1.5 = 3 Marks] [CO1]

- Which of the following are graphic sequences? Provide a construction or proof of impossibility for each of the following: i. (5, 5, 4, 4, 2, 2, 1, 1) ii. (5, 5, 5, 4, 2, 1, 1, 1)
- Prove that there is an n-vertex tournament with indegree equal to outdegree at every vertex if and only if n is odd.

2. [3 Marks] [CO1]

Determine which pairs of graphs below are isomorphic (Figure 1).



a)

b)

c)

Figure 1

3. [1.5 + 1.5 = 3 Marks] [CO1]

Let G be a graph with at least two vertices. Prove or disprove:

- Deleting a vertex of maximum degree cannot increase the average degree.
- Deleting a vertex of minimum degree cannot reduce the average degree.

4. [1.5 + 1.5 = 3 Marks] [CO1]

- Show how to find the maximum spanning tree of a graph, that is, the spanning tree of largest total weight.
- Design algorithm which, given an undirected graph G and a particular edge e in it, determines whether G has a cycle containing e.

5. [1 + 1+ 1 = 3 Marks] [CO4]

- Determine whether the following statement is true or false: 'A knowledge graph must always have an accompanying ontology that has been developed outright'.
- How can you merge nodes and create a relationship between them in Cypher?
- Write Cypher query to find all pairs of people who are exactly 2 hops away from each other in the Movie graph.